

**rationals**<sup>11,40</sup>

STM: test22

STM: mul\_assoc

STM: mul\_wf\_nzero

STM: mul\_nzero

STM: mul\_add\_distrib

ABS: sign( $x$ ) **sign**

STM: sign\_wf

STM: sign-absval

STM: sign-squared

STM: gcd-reduce

ABS: gcd\_reduce( $p; q$ ) **gcd\_reduce**

STM: gcd\_reduce\_wf

STM: gcd\_reduce\_property

STM: coprime-equiv-unique

STM: coprime-equiv-unique-pair

ABS: isint( $z; a; b$ ) **isint def**

ABS: isint\_pair{isint\_pair\_compseq\_tag\_def:ObjectId}  
( $b; a; y; x$ )

**isint\_pair\_compseq\_tag\_def**

ABS: isatom2( $z; a; b$ ) **isatom2**

ABS: isatom2\_pair{isatom2\_pair\_compseq\_tag\_def:ObjectId}  
( $b; a; y; x$ )

**isatom2\_pair\_compseq\_tag\_def**

STM: isint-int

STM: tunion\_wf

ABS:  $A \cup B$  **b-union**

STM: b-union\_wf

ABS:  $\text{qeq}(r; s)$  **peq**

STM: qeq\_wf

STM: qeq-equiv

ABS:  $\mathbb{Q}$  **rationals**

STM: rationals\_wf

STM: int-rational

STM: int\_inc\_rationals

STM: qeq-wf

ABS:  $r + s$  **qadd**

STM: qadd\_wf

STM: qadd-add

ABS:  $r * s$  **qmul**

STM: qmul\_wf

STM: qmul-mul

STM: qminus-minus

ABS:  $1/r$  **qinv**

STM: qinv\_wf

ABS:  $\text{qpositive}(r)$  **qpositive**

STM: qpositive\_wf

ABS:  $\text{qrep}(r)$  **qrep**

STM: qrep\_wf

STM: qeq\_wf2

STM: assert-peq

STM: int-eq-in-rationals

ABS:  $(r/s)$  **qdiv**

STM: qdiv\_wf  
ABS:  $r - s$  **qsub**  
STM: qsub\_wf  
STM: q-elim  
STM: qmul\_ident  
STM: qmul\_com  
STM: qmul\_assoc  
STM: qmul\_inv  
STM: qmul\_inv\_l  
STM: qadd\_ident  
STM: qadd\_com  
STM: qadd\_assoc  
STM: qadd\_minus  
STM: q\_distrib  
STM: qmul\_positive  
STM: qadd\_positive  
STM: qminus\_positive  
STM: q\_trichotomy  
ABS:  $q_{\leq}(r; s)$  **q\_le**  
STM: q\_le\_wf  
ABS:  $\langle \mathbb{Q}^+ \rangle$  **qadd\_grp**  
STM: qadd\_grp\_wf  
STM: mon\_assoc\_q  
STM: mon\_ident\_q  
STM: qinverse\_q  
STM: qinv\_thru\_op\_q  
STM: qinv\_inv\_q

STM: qinv\_id\_q  
STM: qinv\_assoc\_q  
STM: qadd\_inv\_assoc\_q  
STM: qadd\_comm\_q  
STM: qadd\_ac\_1\_q  
STM: qadd\_grp\_wf2  
ABS:  $r < s$  qless  
ABS:  $r \leq s$  qle  
STM: qle\_iff\_lt\_or\_eq\_qorder  
STM: qless\_is\_sp\_of\_leq\_a\_qorder  
STM: qless\_trans\_qorder  
STM: qless\_irreflexivity\_qorder  
STM: qless\_transitivity\_2\_qorder  
STM: qless\_transitivity\_1\_qorder  
STM: qle\_weakening\_eq\_qorder  
STM: qle\_weakening\_lt\_qorder  
STM: qle\_transitivity\_qorder  
STM: qle\_antisymmetry\_qorder  
STM: qless\_complement\_qorder  
STM: qle\_complement\_qorder  
STM: qless\_trichot\_qorder  
STM: grp\_op\_preserves\_le\_qorder  
STM: grp\_op\_preserves\_lt\_qorder  
STM: qless\_irreflexivity  
STM: qle\_antisymmetry  
ABS:  $\langle \mathbb{Q}^+ \rangle$  qrng  
STM: qrng\_wf

STM: qmul\_over\_plus\_qrng  
STM: qmul\_over\_minus\_qrng  
STM: qmul\_zero\_qrng  
STM: qmul\_assoc\_qrng  
STM: qmul\_one\_qrng  
STM: qmul\_comm\_qrng  
STM: qmul\_ac\_1\_qrng  
STM: qdiv-self  
STM: qmul-ident-div  
STM: qmul-zero-div  
STM: qmul-qdiv-cancel  
STM: qmul-qdiv-cancel2  
STM: qmul-qdiv-cancel3  
STM: qmul-qdiv-cancel4  
STM: qmul-preserves-eq  
STM: test-q-norm-conv  
ABS:  $|r|$  **qabs**  
STM: qabs\_wf  
STM: qpositive-qabs  
STM: qabs-zero  
STM: qabs-squared  
STM: qminus-qsub  
STM: qsub-zero  
STM: qsub-sub  
STM: qless\_wf  
STM: qless\_transitivity  
STM: qless\_int

STM: qle\_wf  
STM: qle\_int  
ABS:  $a \geq b$  **qge**  
STM: qge\_wf  
ABS:  $a > b$  **qgt**  
STM: qgt\_wf  
STM: qle\_iff  
STM: assert-qpositive  
STM: qmul-positive  
STM: qminus-positive  
STM: decidable\_equal\_rationals  
STM: decidable\_qle  
STM: decidable\_qless  
ABS:  $q\_less(a;b)$  **q\_less**  
STM: q\_less\_wf  
STM: assert-q\_less  
STM: assert-q\_less\_eq  
STM: assert-q\_le  
STM: assert-q\_le\_eq  
STM: qmul\_zero  
STM: qmul\_non\_neg  
STM: non-neg-qmul  
STM: q-square-non-neg  
STM: qadd\_preserves\_qless  
STM: qadd\_preserves\_qle  
STM: qadd\_preserves\_eq  
STM: qmul\_preserves\_qless

STM: qmul\_preserves\_qle  
 STM: qadd\_functionality\_wrt\_qle  
 STM: qadd\_functionality\_wrt\_qless  
 STM: qadd\_functionality\_wrt\_qless\_2  
 STM: qle\_functionality\_wrt\_implies  
 STM: qless\_functionality\_wrt\_implies\_1  
 STM: qmul\_functionality\_wrt\_qle  
 STM: qmul-qdiv  
 STM: qless-minus  
 STM: qle-minus  
 STM: qinv-positive  
 STM: qinv-negative  
 STM: qinv-zero  
 STM: qdiv-qdiv  
 STM: q-ineq-test  
 STM: qadd-non-neg  
 ABS: qdist( $r;s$ ) **qdist**  
 STM: qdist\_wf  
 ABS:  $a \leq b \leq c$  **qbetween**  
 STM: qbetween\_wf  
 ABS:  $a < b < c$  **q-between**  
 STM: q-between\_wf  
 STM: qle-normalize  
 STM: qle\_reflexivity  
 STM: qbetween-qdist  
 ABS:  $\Sigma a \leq j < b. E(j)$  **qsum**  
 STM: qsum\_wf

ABS:  $r \uparrow n$  **qexp**

STM: qexp\_wf

STM: exp\_zero\_q

STM: exp\_unroll\_q

STM: sum\_unroll\_base\_q

STM: sum\_unroll\_hi\_q

STM: sum\_unroll\_unit\_q

STM: sum\_unroll\_lo\_q

STM: sum\_shift\_q

STM: sum\_split\_q

STM: sum\_plus\_q

STM: prod\_sum\_l\_q

STM: prod\_sum\_r\_q

STM: binomial\_q

STM: sum\_of\_geometric\_prog\_q

STM: qsum-int

STM: qsum-qle

ABS:  $\delta(i;j)$  **delta**

STM: delta\_wf

STM: qsum-delta

STM: summand-qle-sum

STM: qexp-positive

STM: qexp-one

STM: qsum-const

STM: qsum-const2

STM: q-geometric-series

STM: qsum-reciprocal-squares

STM: qsum-reciprocal-squares-bound  
STM: q-archimedean  
STM: qsum-non-neg  
STM: qsum-non-neg2  
STM: qsum-subsequence-qle  
STM: q-not-limit-zero-diverges  
STM: q-not-limit-zero-diverges-2  
STM: q-min-exists  
STM: q-max-exists  
ABS:  $q\text{-linear}(k; i.X(i); y)$  **q-linear**  
STM: q-linear\_wf  
STM: q-linear-base  
STM: q-linear-unroll  
STM: q-linear-sum  
STM: q-linear-times  
STM: q-linear-equal  
ABS:  $q\text{-rel}(r; x)$  **q-rel**  
STM: q-rel\_wf  
STM: decidable\_\_q-rel  
ABS:  $q\text{-rel-lub}(r_1; r_2)$  **q-rel-lub**  
STM: q-rel-lub\_wf  
STM: q-constraint-times  
STM: q-constraint-sum  
STM: q-constraint-zero  
STM: q-constraint-positive  
STM: q-constraint-negative  
ABS:  $q\text{-constraints}(k; A; y)$  **q-constraints**

STM: q-constraints\_wf  
STM: product-map  
STM: null-map  
STM: average-qbetween  
STM: average-q-between  
STM: rational-has-value  
ABS: *as*[*i*]?*a* select?  
STM: select?\_wf  
ABS: normalize-constraint(*k;p*) **normalize-constraint**  
STM: normalize-constraint\_wf  
STM: normalize-constraint-eq  
ABS: normalize-constraints(*k;A*) **normalize-constraints**  
STM: normalize-constraints\_wf  
STM: normalize-constraints-eq  
STM: decidable\_\_q-constraints  
STM: decidable\_\_q-constraints\_cv  
STM: decidable\_\_q-constraints-opt  
ABS: qdot(*as;bs*) **qdot**  
STM: qdot\_wf  
ABS: q-sat-constraints(*k;A;y*) **q-sat-constraints**  
STM: q-sat-constraints\_wf  
STM: decidable\_\_q-constraints2  
STM: test23  
ABS: test\_case1() **test\_case1**  
STM: test\_case1\_wf  
STM: int\_nzero-rational